

$$a) \sqrt{2x+5} + \sqrt{3x-5} = 4,$$

$$b) \sqrt[3]{x} + \sqrt[3]{3x-2} = \sqrt[3]{x-2},$$

$$c) \frac{(4-x)\sqrt{4-x} + (x-2)\sqrt{x-2}}{\sqrt{4-x} + \sqrt{x-2}} = 2,$$

$$d) \sqrt{x-2} + \sqrt{x+2} + 2\sqrt{(x-2)(x+2)} = 6 - 2x,$$

$$e) \sqrt{x-1} + \sqrt{3-x} = x^2 - 4x + 6,$$

$$f) \sqrt[4]{x+7} - \sqrt[4]{x-9} = 2,$$

$$g) \frac{x^2}{\sqrt{2x+15}} + \sqrt{2x+15} = 2x,$$

$$h) 3\sqrt{x^2-9} + 4\sqrt{x^2-16} + 5\sqrt{x^2-25} = \frac{120}{x},$$

$$i) \sqrt{x(x+1)} = \sqrt{x+3} - \sqrt{1 + \frac{1}{x^2}}.$$

Fig.1

a)

$$A = \begin{pmatrix} 1 & -2 & 3 \\ 2 & 1 & 2 \\ 4 & 2 & 4 \\ 3 & -6 & 9 \end{pmatrix}$$

b)

$$\begin{aligned} \Delta(n) &= \begin{vmatrix} n & n-1 & n-2 & \dots & 3 & 2 & \sum_{k=1}^n kx^{k-1} \\ -1 & x & 0 & \dots & 0 & 0 & -x^n + x^{n-1}x \\ 0 & -1 & x & \dots & 0 & 0 & -x^{n-1} + x^{n-2}x \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & 0 & \dots & -1 & x & -x^3 + x^2x \\ 0 & 0 & 0 & \dots & 0 & 1 & -x^2 + xx \end{vmatrix} \\ &= \left(\sum_{k=1}^n kx^{k-1} \right) \cdot \begin{vmatrix} -1 & x & 0 & \dots & 0 & 0 \\ 0 & -1 & x & \dots & 0 & 0 \\ \dots & \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & 0 & \dots & -1 & x \\ 0 & 0 & 0 & \dots & 0 & 1 \end{vmatrix} \\ &= (-1)^{n-1} \sum_{k=1}^n kx^{k-1} \end{aligned}$$

Fig.2

$$\begin{array}{ll}
 1. \left[(\sqrt[3]{5})^{\sqrt{5}} \right]^{-3\sqrt{5}} & 4. \frac{\sqrt{a^3 \sqrt{a} \sqrt{a}}}{\sqrt{a^3 \sqrt{a^4 \sqrt{a}}}} \\
 2. \left(\frac{\sqrt{a}}{3} + \frac{3}{\sqrt[3]{a}} \right)^{13} & \\
 3. \left(\sqrt[5]{x} + \frac{1}{\sqrt{x}} \right)^{21} & \\
 5. \frac{\sqrt{\frac{abc+4}{a} - 4\sqrt{\frac{bc}{a}}}}{\sqrt{abc}-2} = \frac{1}{\sqrt{a}} & \\
 6. \frac{\sqrt[4]{x}}{12\sqrt[12]{y^{19}}} * \left(\frac{x^{\frac{1}{2}} \sqrt[3]{y}}{\sqrt[4]{xy^{-1}}} \right)^{\frac{1}{3}} * \left(\frac{x^{-\frac{3}{8}}}{y^{-\frac{2}{3}}} \right)^{\frac{4}{3}} &
 \end{array}$$

Fig.3

$$(1+x)^n = 1 + \frac{nx}{1!} + \frac{n(n-1)x^2}{2!} + \dots$$

Fig.4

$$7. 9^x = \frac{1}{729}$$

$$8. 3^x = \sqrt[3]{9}$$

$$9. 4^{\sqrt{x+1}} = 64 * 2^{\sqrt{x+1}}$$

$$10. \sqrt[2]{8^{x-1}} = \sqrt[3]{4^{2-x}}$$

$$11. \left(\frac{3}{5}\right)^{x+1} + \left(\frac{3}{5}\right)^{1-x} = 1,2$$

$$12. (\sqrt{5})^{\frac{1}{2}}$$

Fig.5

$$\frac{2x+4}{x-1} + (2x+3)$$

$$\begin{cases} 2x+7 < 0 \\ 4x^2+x \geq 7 \end{cases}$$

$$\sqrt[n]{4x + \frac{x_2+x_1}{2x+1}}$$

$$2 \pm \sin x + \frac{\tan x}{\cos y} \geq \alpha$$

$$\textcolor{red}{\Omega} + \pi = \beta$$

Fig.6