

Variantă 88
III.

13. a)
$$\begin{cases} a = \frac{-476}{238} = -2 \\ c = \frac{5}{9} \cdot \frac{9}{5} = 1 \end{cases} \Rightarrow a + c = -2 + 1 = -1 \in \mathbf{Z}.$$

b) $b = \frac{\sqrt{4} - \sqrt{5} + \sqrt{5} - \sqrt{6} + \sqrt{6} - \sqrt{7} + \sqrt{7} - \sqrt{8} + \sqrt{8} - \sqrt{9}}{-1} = \frac{2 - 3}{-1} = 1 \Rightarrow a + b + c = 0.$

14. a)
$$\begin{cases} f(-1) = 5 \\ f(0) = 4 \end{cases} \Leftrightarrow \begin{cases} -a + b = 5 \\ b = 4 \end{cases} \Leftrightarrow \begin{cases} a = -1 \\ b = 4 \end{cases} \Rightarrow f(x) = -x + 4.$$

b) $AB = \sqrt{AC^2 + BC^2} = \sqrt{1+1} = \sqrt{2}$, unde punctul $C(0;5)$.

c) $f(x) = -x + 4 \Leftrightarrow M(x; y) \in G_f; x = y \Rightarrow x = -x + 4 \Leftrightarrow x = 2 \Rightarrow M(2;2).$

15. b) $r = 15$ și $\frac{r}{3} = \frac{h}{4} = \frac{g}{5} \Rightarrow h = 20$ cm.

c) $A_l = 1125\pi \text{ cm}^2$.

d) $\frac{VO'}{VO} = \frac{r}{R} \Leftrightarrow \frac{VO'}{VO} = \frac{1}{2} \Leftrightarrow \frac{VO - 20}{VO} = \frac{1}{2} \Rightarrow VO = 40$ cm. $V_{con} = 12000\pi \text{ cm}^3$.